

B.A. (Honours) Examination, 2023

Semester—II (CBCS)

Subject: Economics

Course-CC-4(Mathematical Methods for Economics)

Time: 3 hours

Full Marks: 60

Questions are of value as indicated in the margin

UNIT-I

Answer any two questions from the following:

15x2=30

- Qs1. (i) Find  $x, y, z, t$  where  $3 \begin{bmatrix} x & y \\ z & t \end{bmatrix} = \begin{bmatrix} x & 6 \\ -1 & 2t \end{bmatrix} + 4 \begin{bmatrix} 4 & x+y \\ z+t & 3 \end{bmatrix}$
- (ii) Suppose  $A = \begin{bmatrix} 1 & 2 \\ 3 & -4 \end{bmatrix}$  and  $g(x) = x^2 + 3x - 10$ , then show that A is zero of the polynomial  $g(x)$ .
- (iii) Show that the inverse of the matrix  $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$  is equal to  $B = \frac{1}{\det A} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$  4 + 5 + 6 = 15
- Qs.2. (i) Suppose A is a square matrix. Write A as the sum of a symmetric and a skew-symmetric matrix.
- (ii) Let A be an arbitrary 2x2 orthogonal matrix. Prove that if (a, b) is the first row of A then  $a^2 + b^2 = 1$  and  $A = \begin{bmatrix} a & b \\ -b & a \end{bmatrix}$  or  $A = \begin{bmatrix} a & b \\ b & -a \end{bmatrix}$ .
- (iii) Find a 2x2 orthogonal matrix P whose first row is a multiple of (3, -4). 5 + 5 + 5 = 15
- Qs.3. (i) Compute the Adjoint of the matrix  $A = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 3 & 5 \\ 1 & 5 & 12 \end{bmatrix}$ .
- (ii) Solve the given equations by Matrix method:  $3x - 2y = 4, 4x - 3y = 5$ .
- (iii) Is the system of equations;  $x + y + z = 4, 2x + 5y - 2z = 3, x + 7y - 7z = 5$  solvable? 6 + 5 + 4 = 15
- Qs.4. (i) Show that  $\begin{vmatrix} a & b & c \\ a^2 & b^2 & c^2 \\ b+c & c+a & a+b \end{vmatrix} = (b-c)(c-a)(a-b)(a+b+c)$ .
- (ii) Solve the equation:  $\begin{vmatrix} x+1 & -3 & 4 \\ -5 & x+2 & 2 \\ 4 & 1 & x-6 \end{vmatrix} = 0$
- (iii) Solve by Cramer's rule:  $x + 2y + 3z = 6, 2x + 4y + z = 7, 3x + 2y + 9z = 14$ . 5 + 5 + 5 = 15

UNIT-II

Answer any two questions from the following:

15x2 = 30

- Qs.5. Define Saddle Point. Obtain the Linear and quadratic approximations of the following function near the point (0, 0):  
 $f(x, y) = \cos x + \sin 2y$  2+13 = 15
- Qs.6. (a) Suppose your objective function is  $f(x, y) = 2x^2 + y^2$  and the constraint is  $xy = 2$ . Find the optimum values using Lagrange multiplier.
- (b) Verify the envelop theorem in the function  $f(x) = 2x^2 + 8kx + 3k^2$ , where 'k' is a parameter 8+7 = 15
- Qs.7. Suppose a consumer maximizes its utility  $Q = X^\alpha Y^{1-\alpha}$  subject to her budget  $M = P_x X + P_y Y$  where all symbols follow their usual meanings. Derive the maximum value function and then prove the Euler's theorem. Find the critical point(s) of the given objective function.
- Qs.8. Find the critical point(s) of the following functions, and use the second partials test to obtain any local extrema or saddle point(s):  
 $f(x, y) = 2x^2 + 6y^2 + 12x - 24y + 30$  7+5+3 = 15
- 3+12 = 15